

WINDOWING, SMOOTHING, FILTERING... CONVOLUTION!

YU / HUGHES

OCTOBER 05, 2021



UMASS
AMHERST

FO DETECTION

WAYS TO ESTIMATE F0: REVIEW QUESTION

- ▶ Download this WAV file.

<https://drive.google.com/open?id=0BxrcL0TA8FhYY2V3SWdlZjA4UVE>

- ▶ Estimate the f_0 in the two [ma] syllables in three ways. Make TextGrids to segment out each [ma] syllable.
- ▶ Measurement methods
 - ▶ Off of the waveform: based on cycle-to-cycle distance
 - ▶ Off of the spectrum: spacing between harmonics
 - ▶ Off of the narrow-band spectrogram

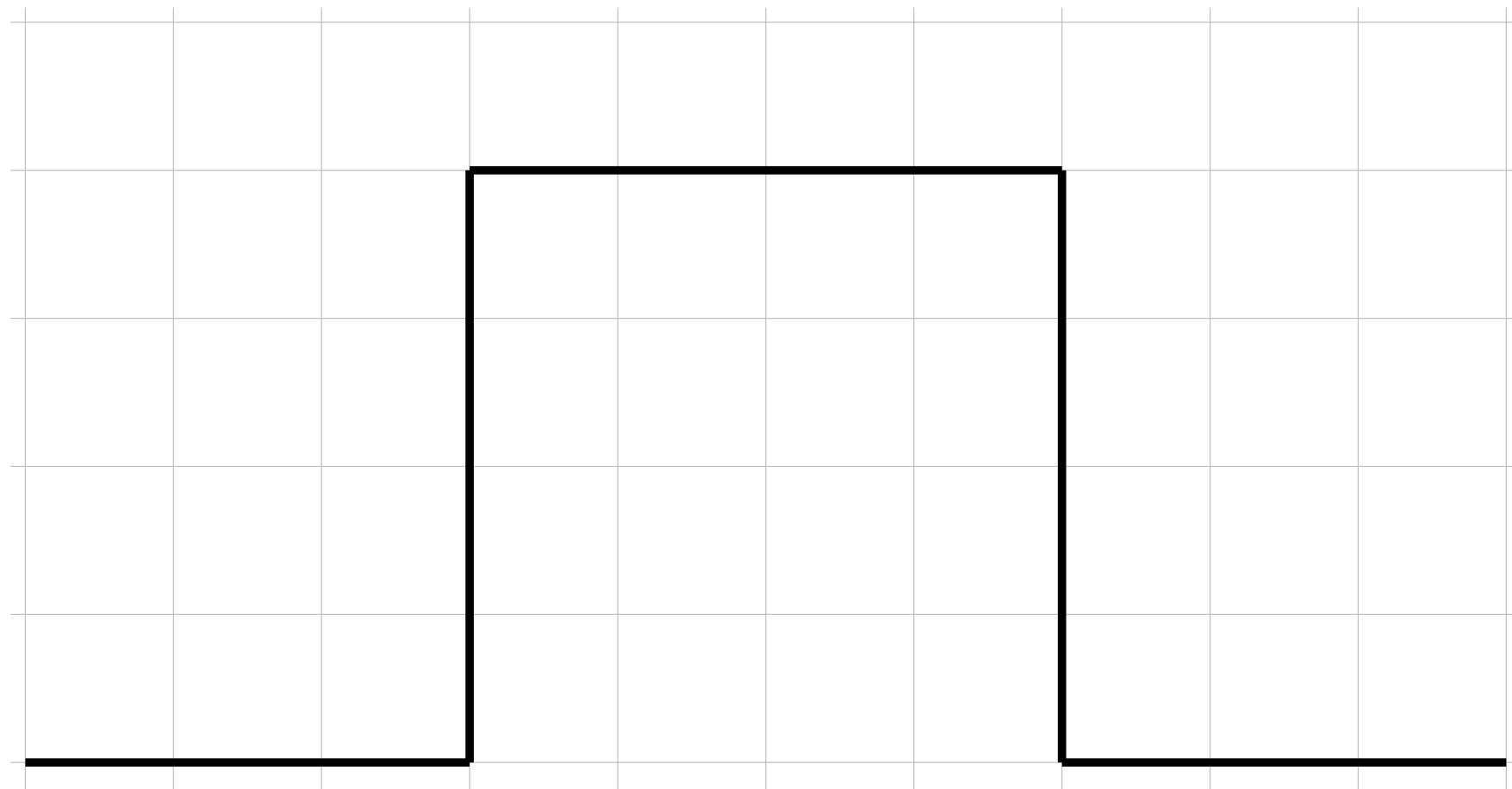
WAYS TO ESTIMATE F0

▶ **Measurement methods**

- ▶ Off of the waveform: based on cycle-to-cycle distance
- ▶ Off of the spectrum: spacing between harmonics
- ▶ Off of the narrow-band spectrogram (demo)

Note these all involve visual inspection!
How does a computer "see" f0?

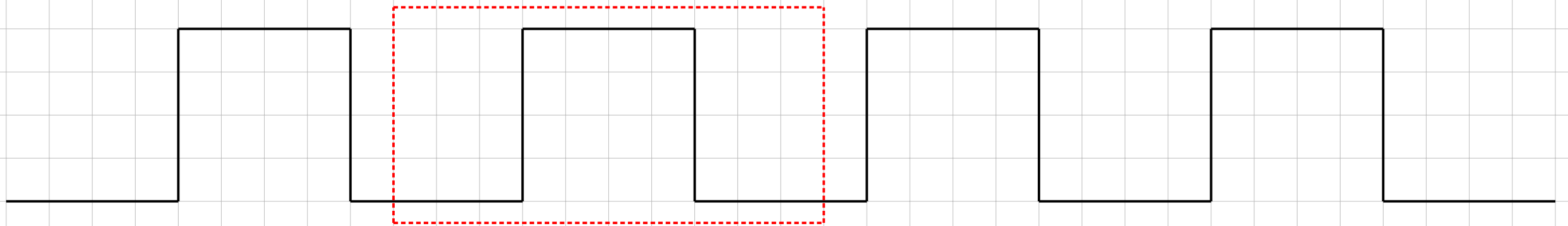
PRAAT FO DETECTION EXERCISE



One cycle of a “square” wave

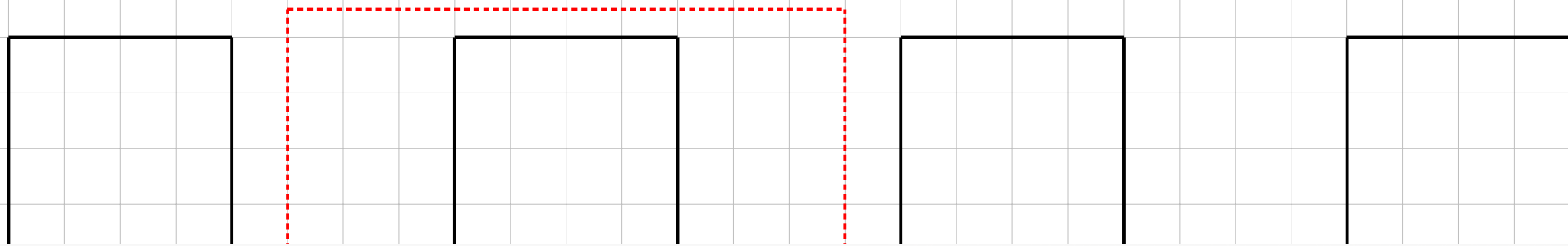
PRAAT FO DETECTION EXERCISE

What's the period of this waveform?



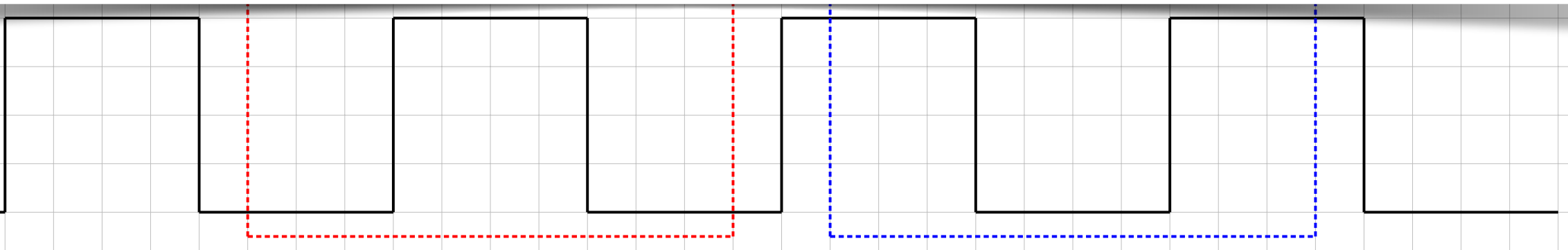
PRAAT FO DETECTION EXERCISE

What's the period of this waveform?



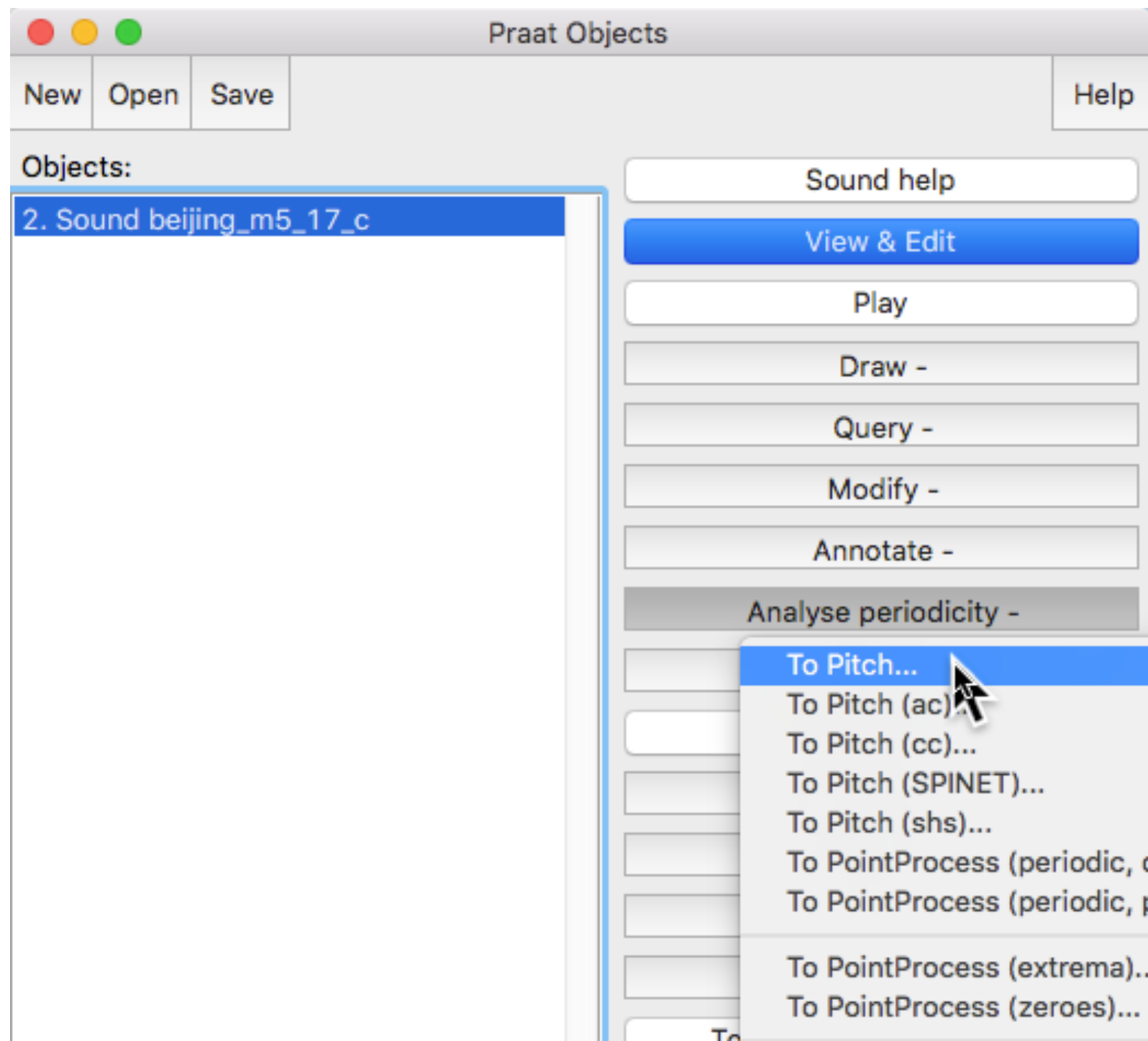
How can a computer tell when a pattern repeats?

Our eyes are wonderful pattern detectors, but computers don't have eyes.



WHAT CAN GO WRONG WITH F0 DETECTION?

► Create “pitch object” in Praat



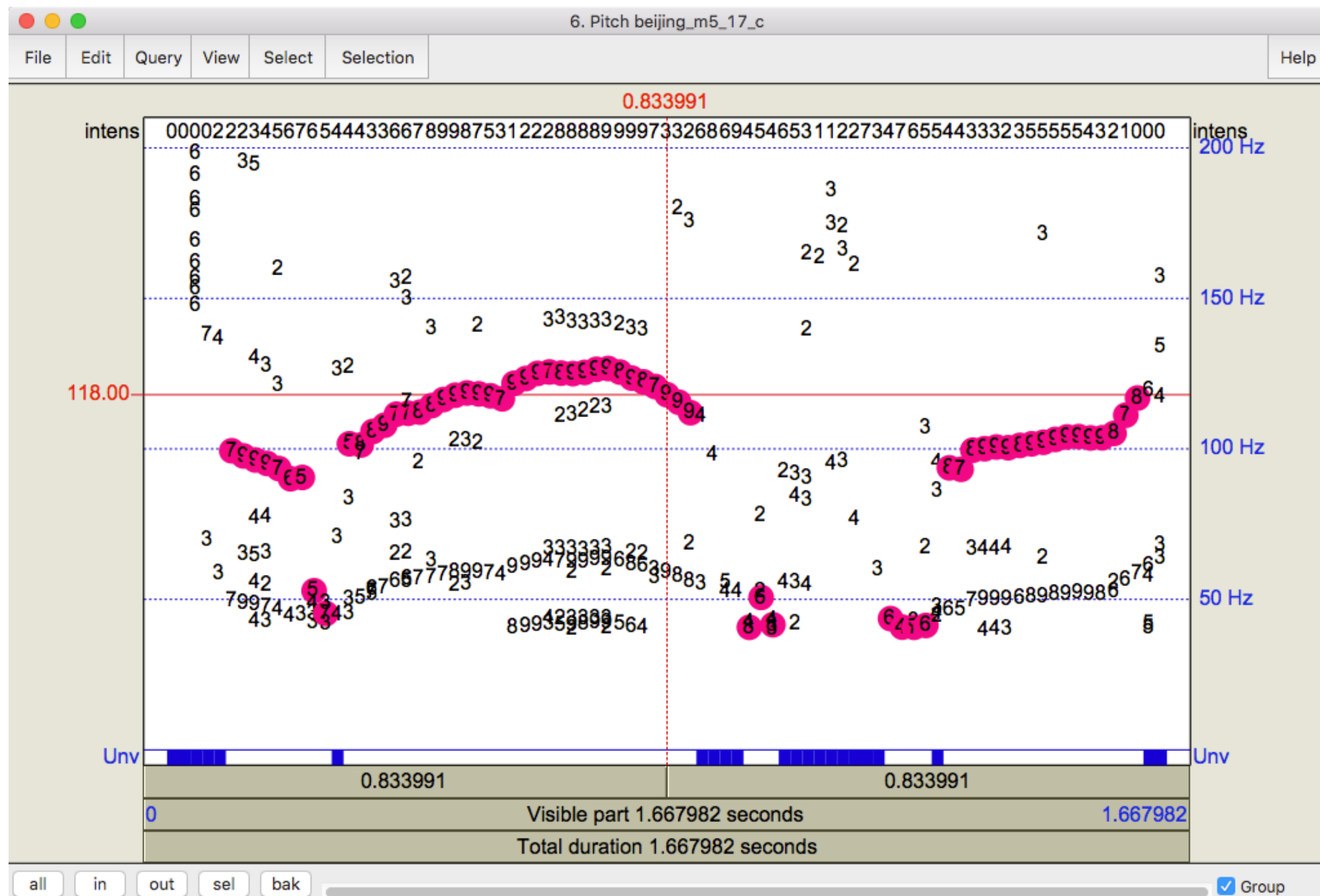
WHAT CAN GO WRONG WITH F0 DETECTION?

- ▶ **Select appropriate lower and upper bounds for what f0 values Praat should consider as possible candidates**
- ▶ To investigate creak, drop pitch floor to 40 Hz
- ▶ Pitch ceiling: depends on pitch range of speaker

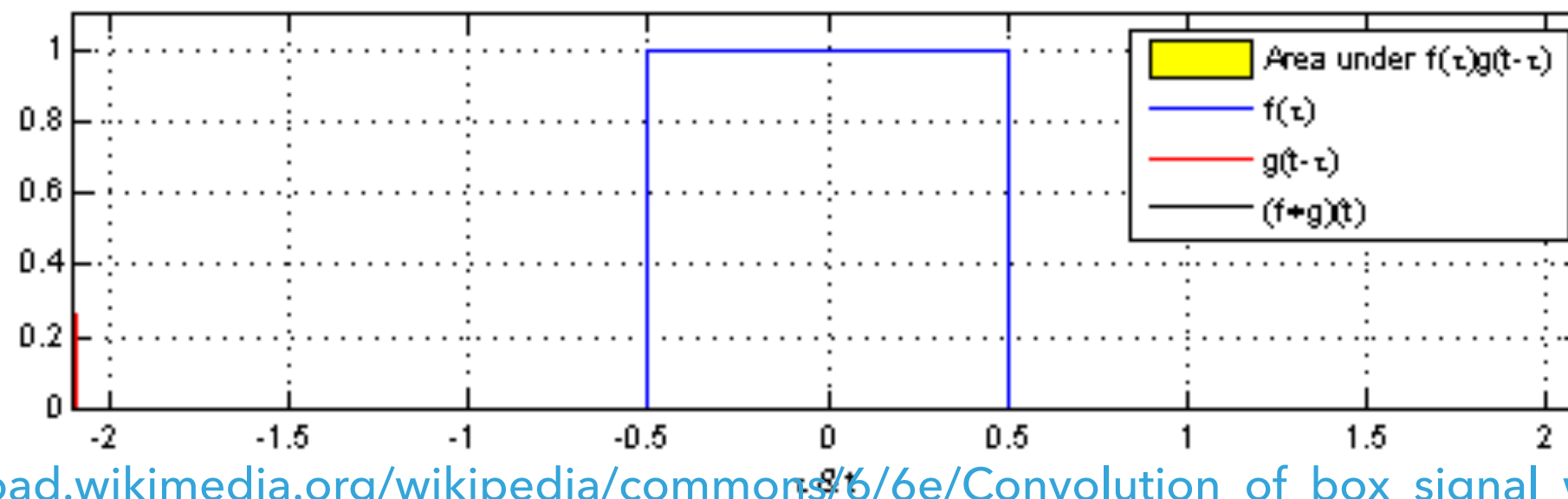


WHAT CAN GO WRONG WITH F0 DETECTION?

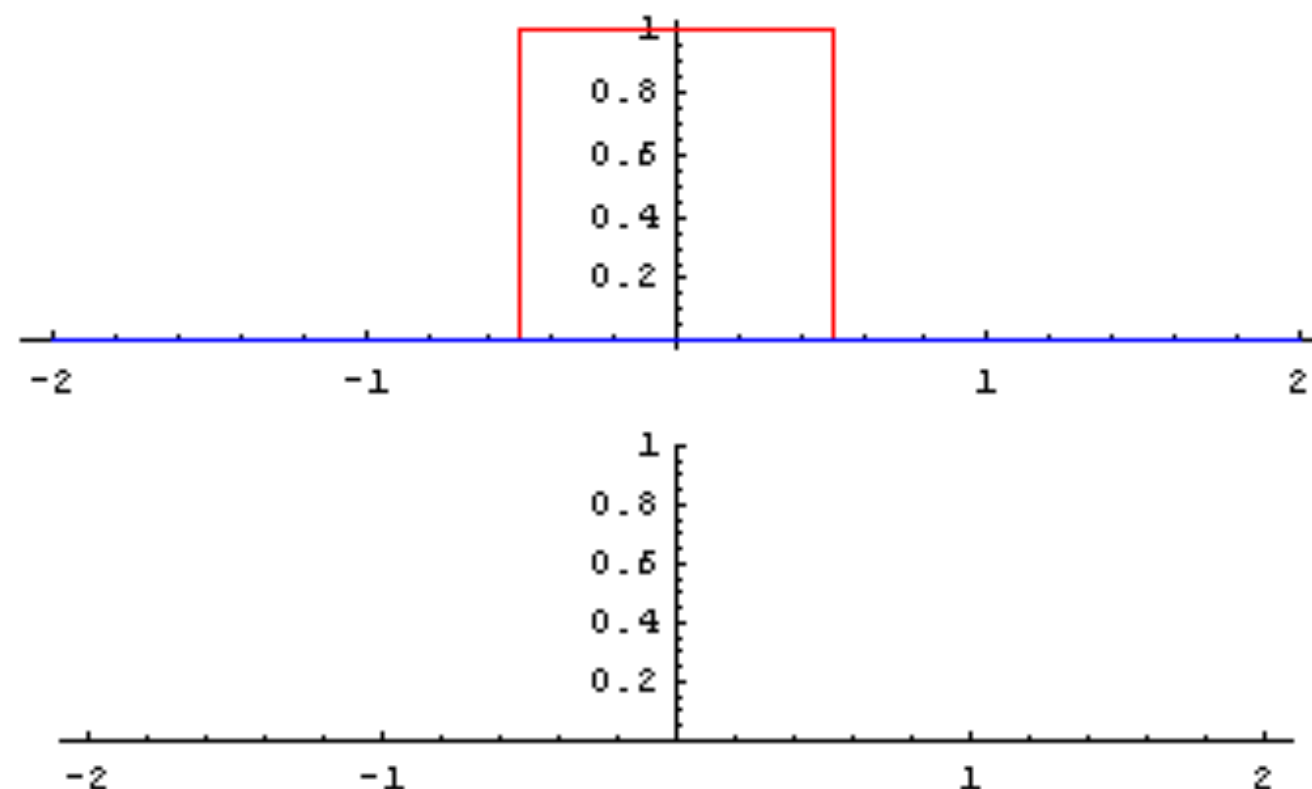
► Explore the Pitch object



AUTOCORRELATION

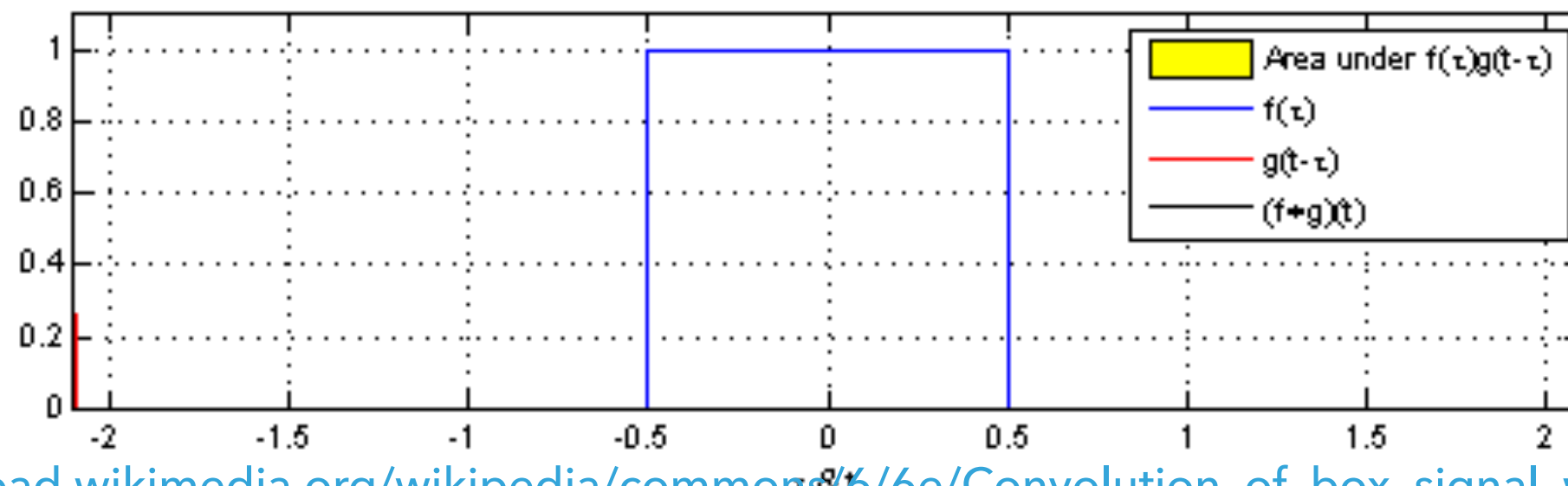


https://upload.wikimedia.org/wikipedia/commons/6/6e/Convolution_of_box_signal_with_itself.gif

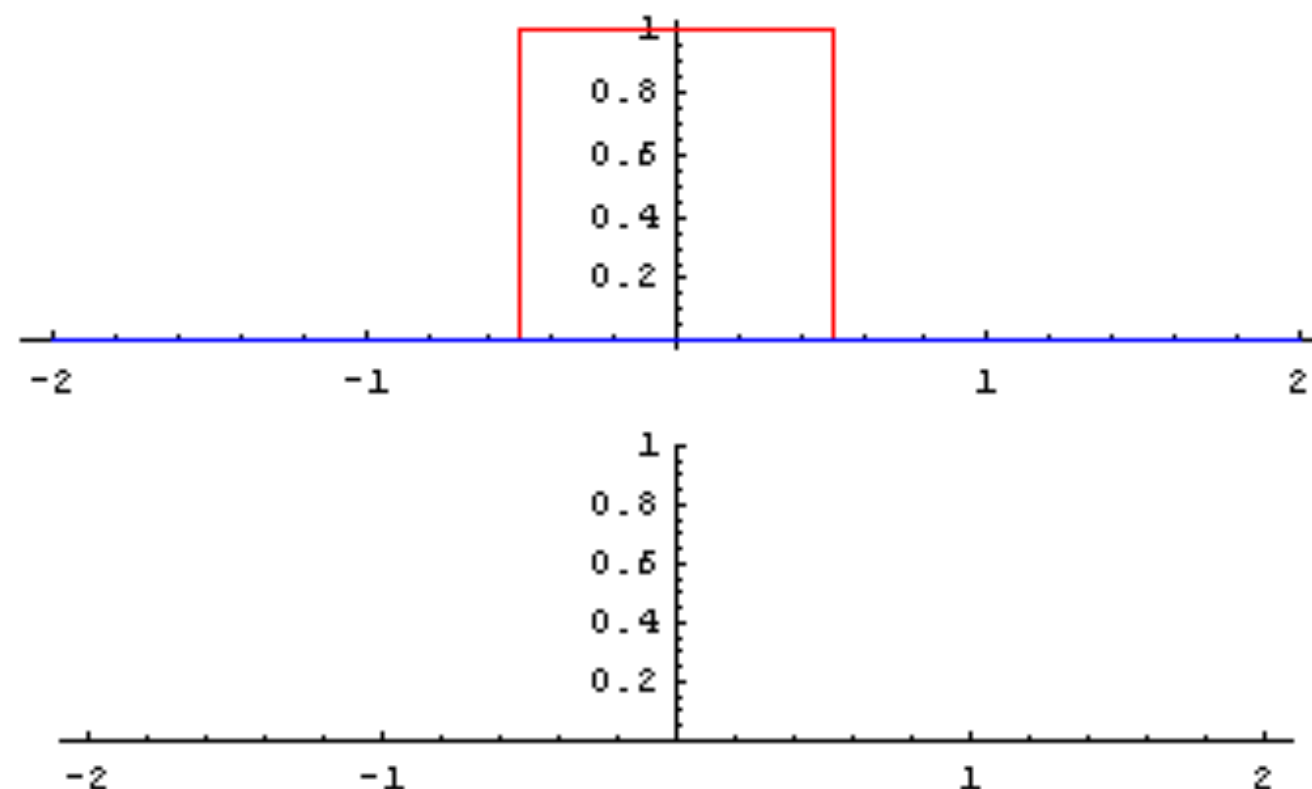


https://commons.wikimedia.org/wiki/Category:Convolution#/media/File:Convolucion_Funcion_Pi.gif

AUTOCORRELATION

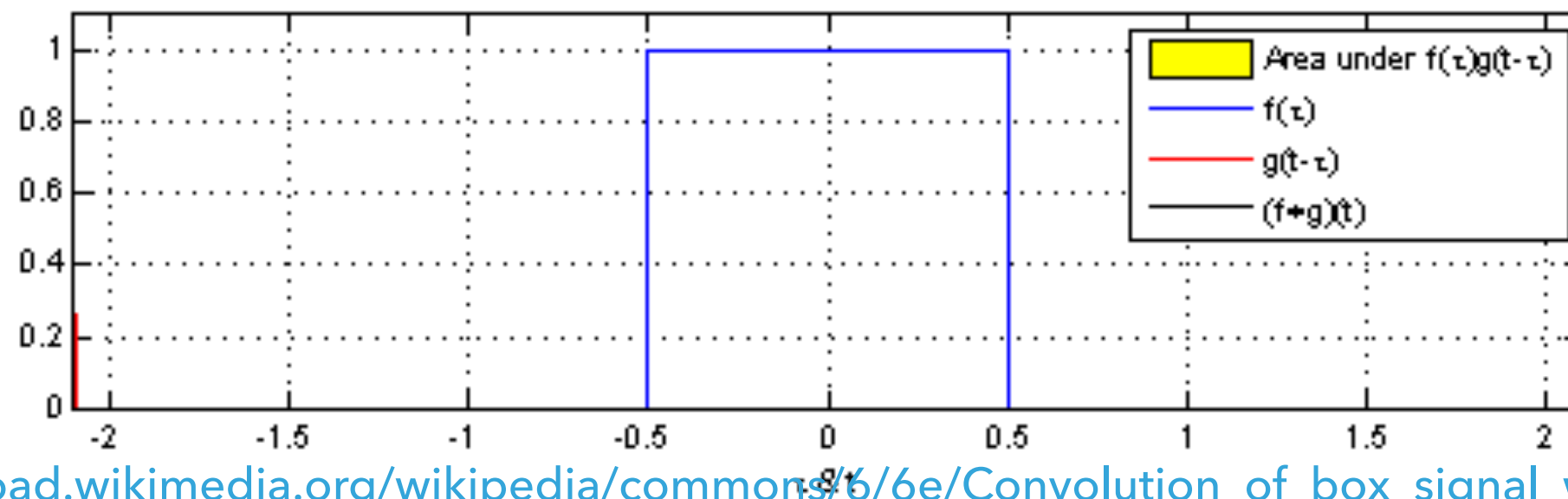


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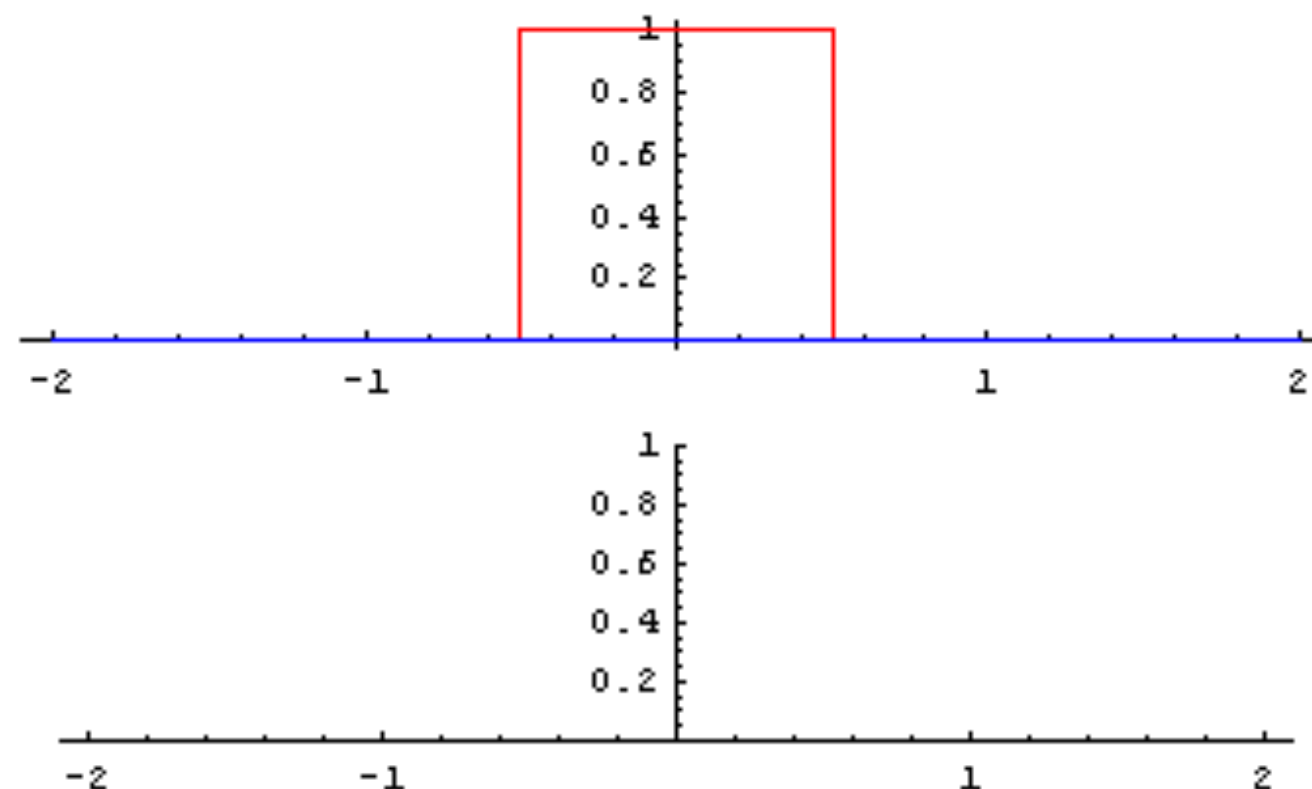


https://commons.wikimedia.org/wiki/Category:Convolution#/media/File:Convolucion_Funcion_Pi.gif

AUTOCORRELATION

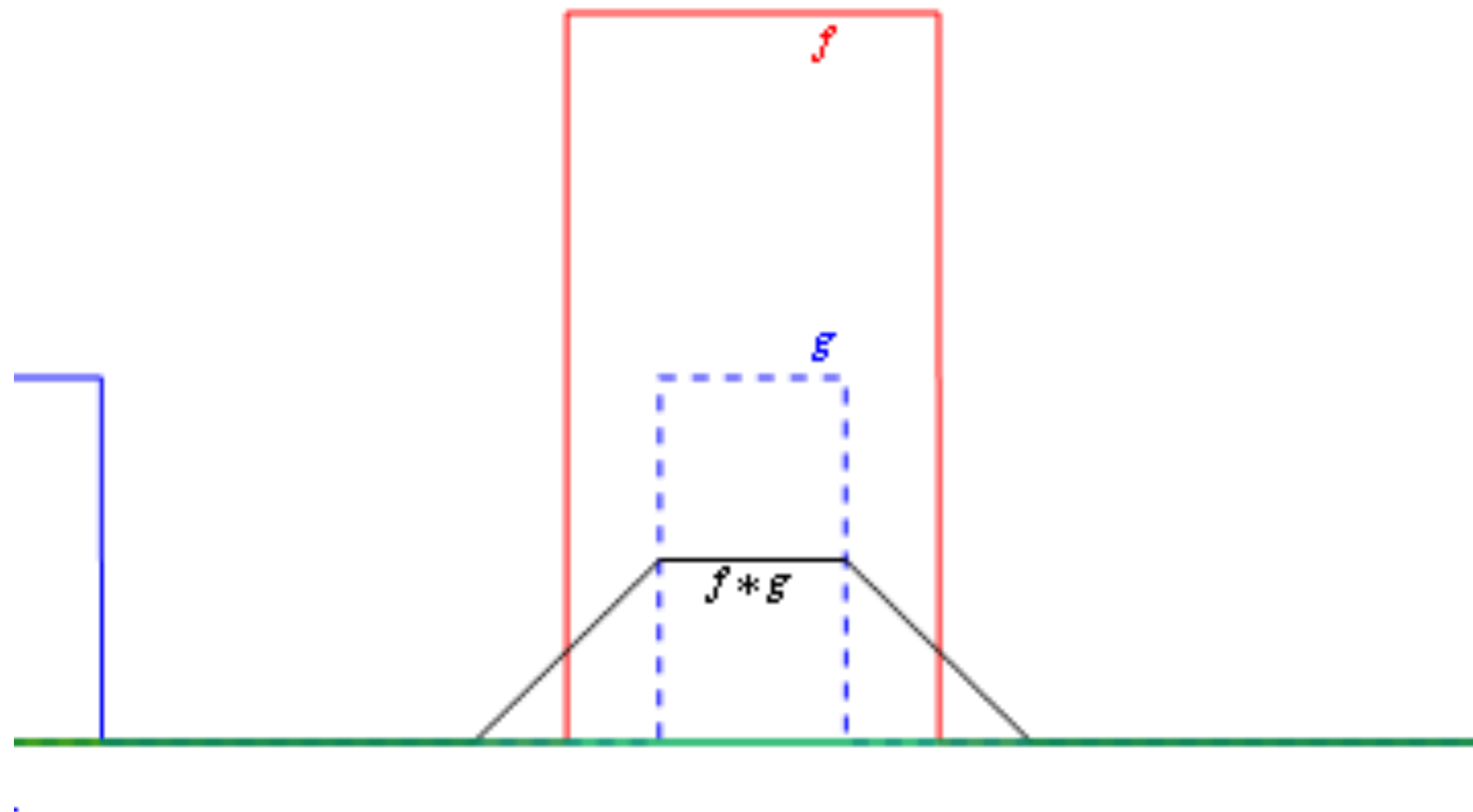


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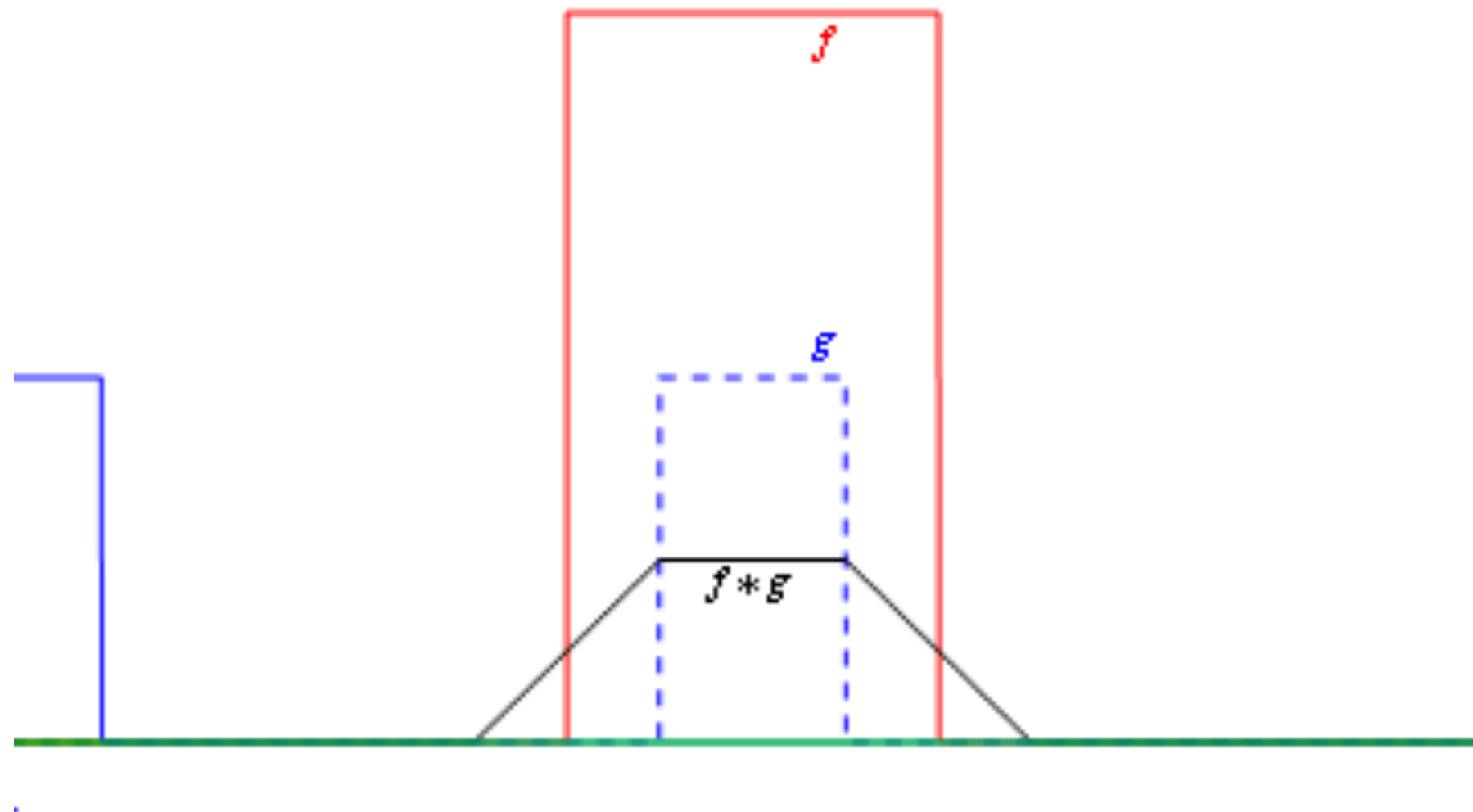


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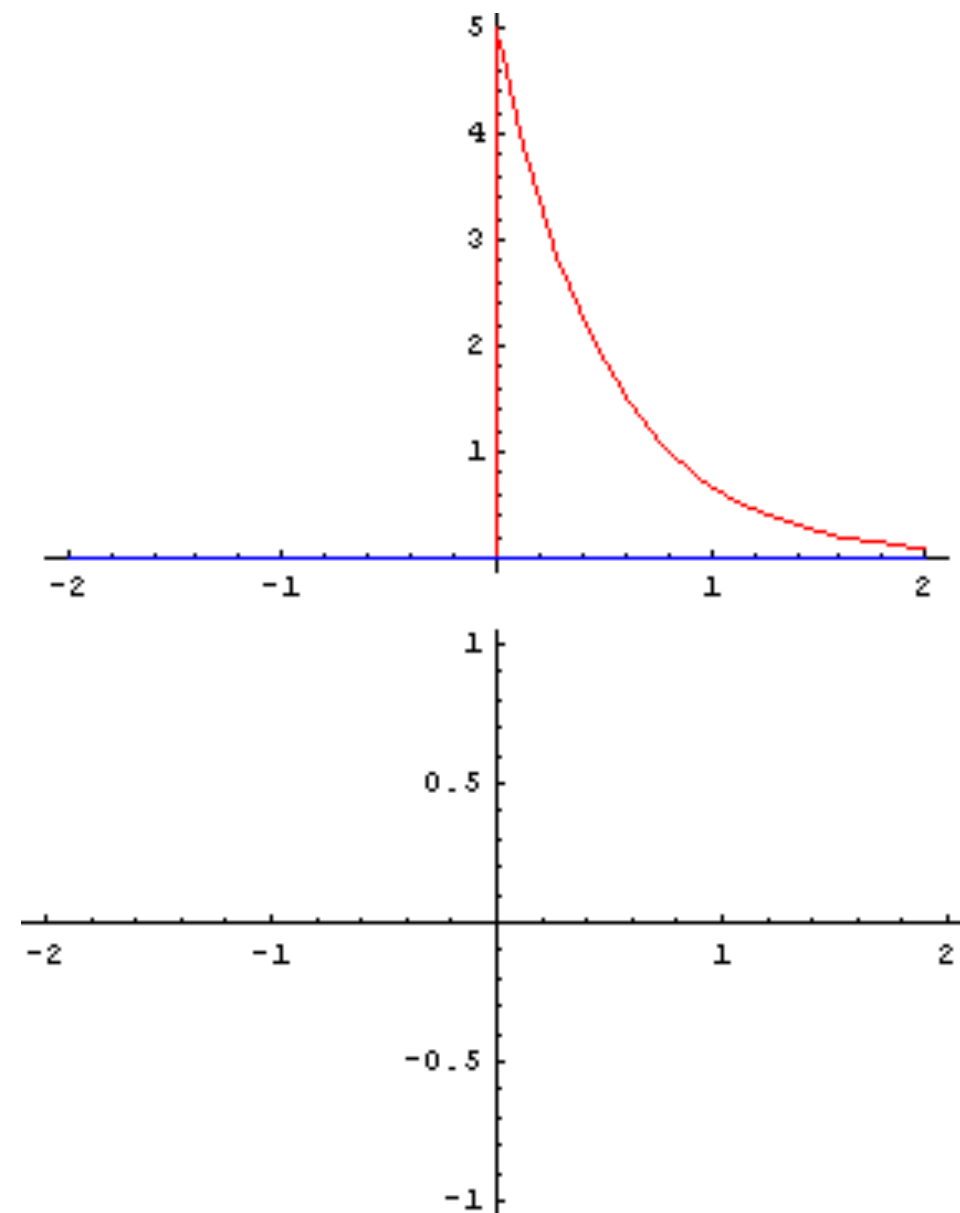
TWO DIFFERENT BOXCARS...



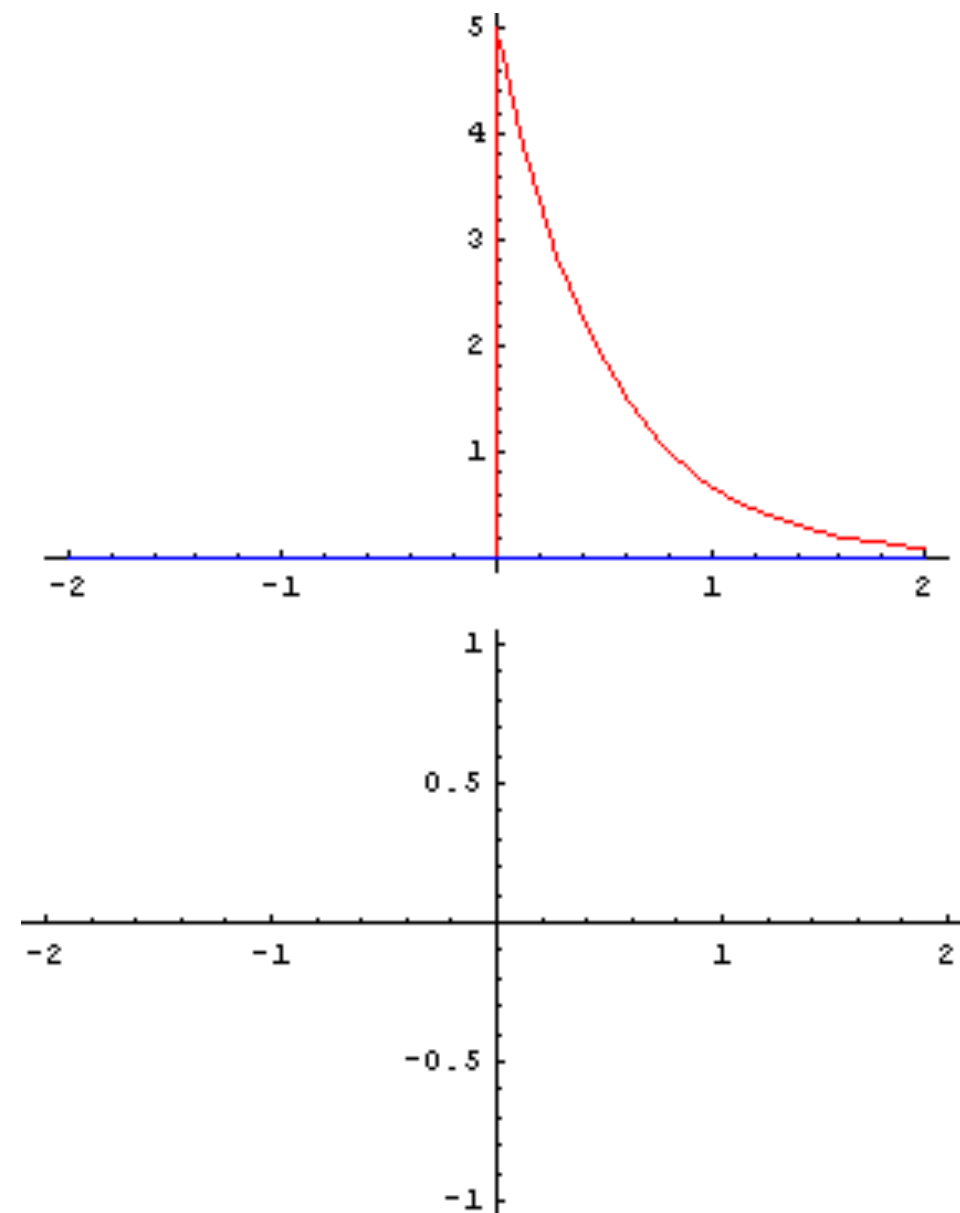
TWO DIFFERENT BOXCARS...



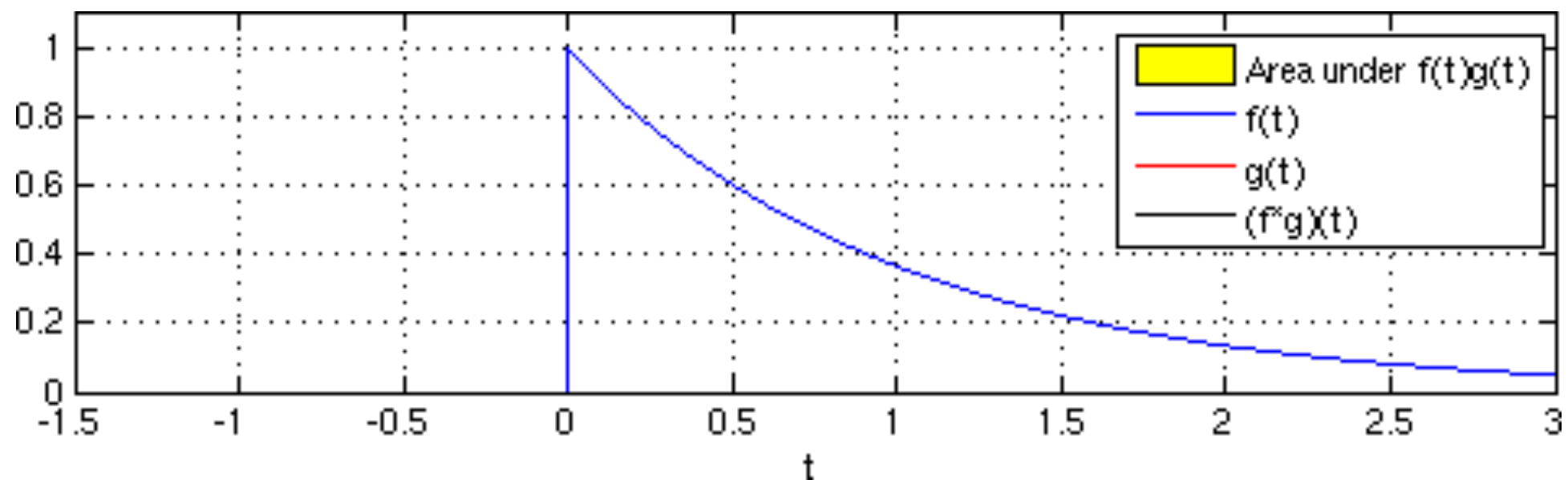
A BOX AND A SPIKY FUNCTION



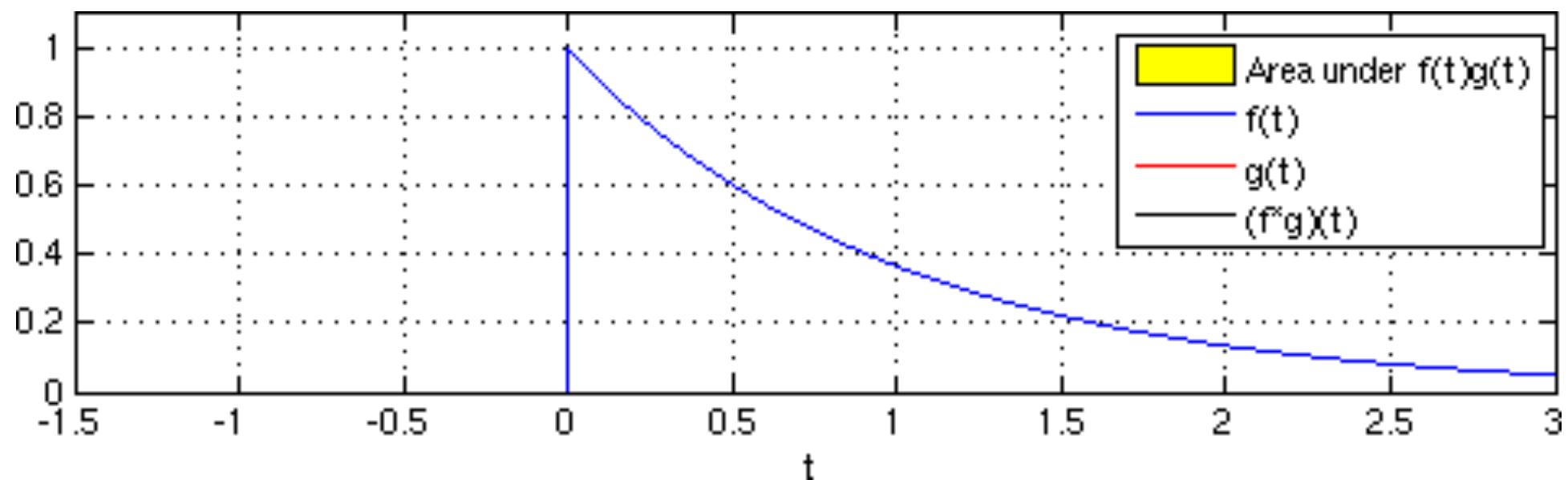
A BOX AND A SPIKY FUNCTION



A BOX AND A SPIKY FUNCTION

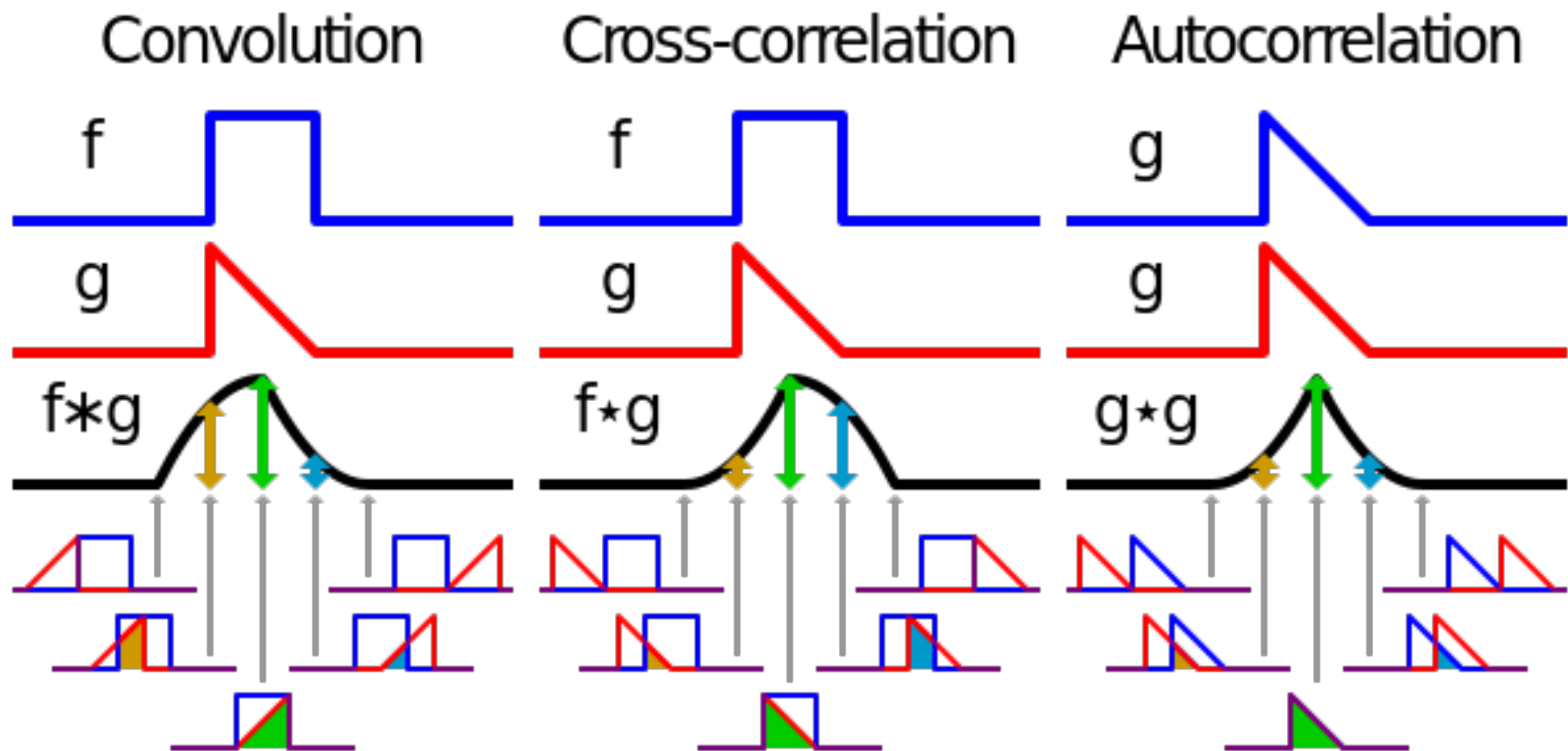


A BOX AND A SPIKY FUNCTION



CONVOLUTION

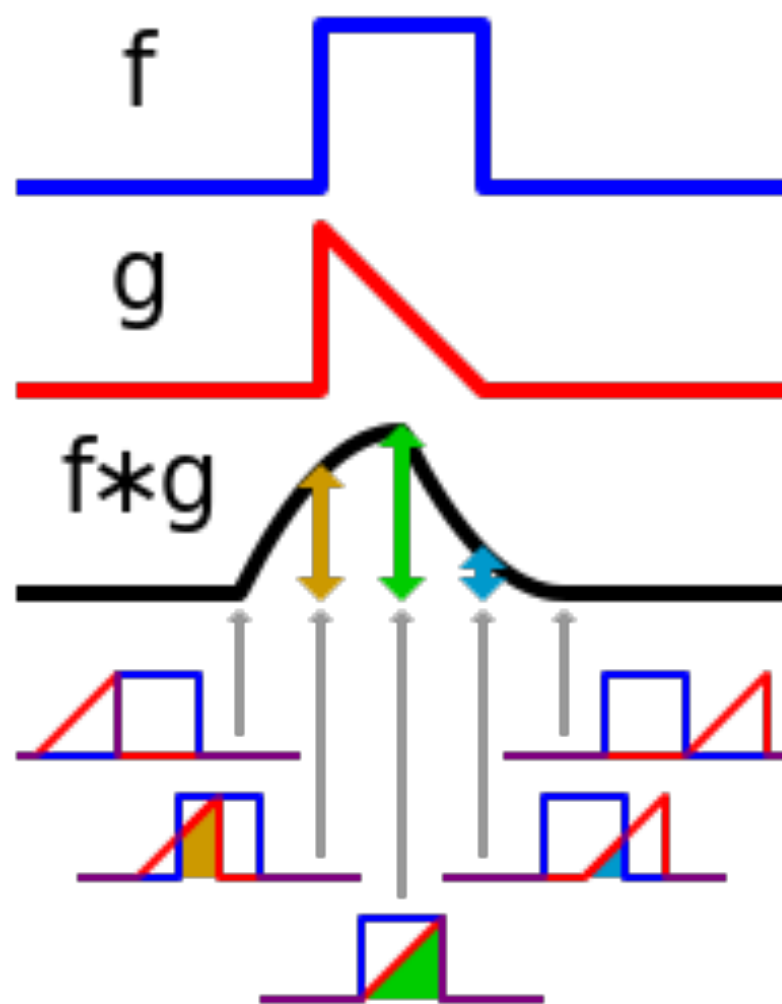
STARS OF DIGITAL SIGNAL PROCESSING



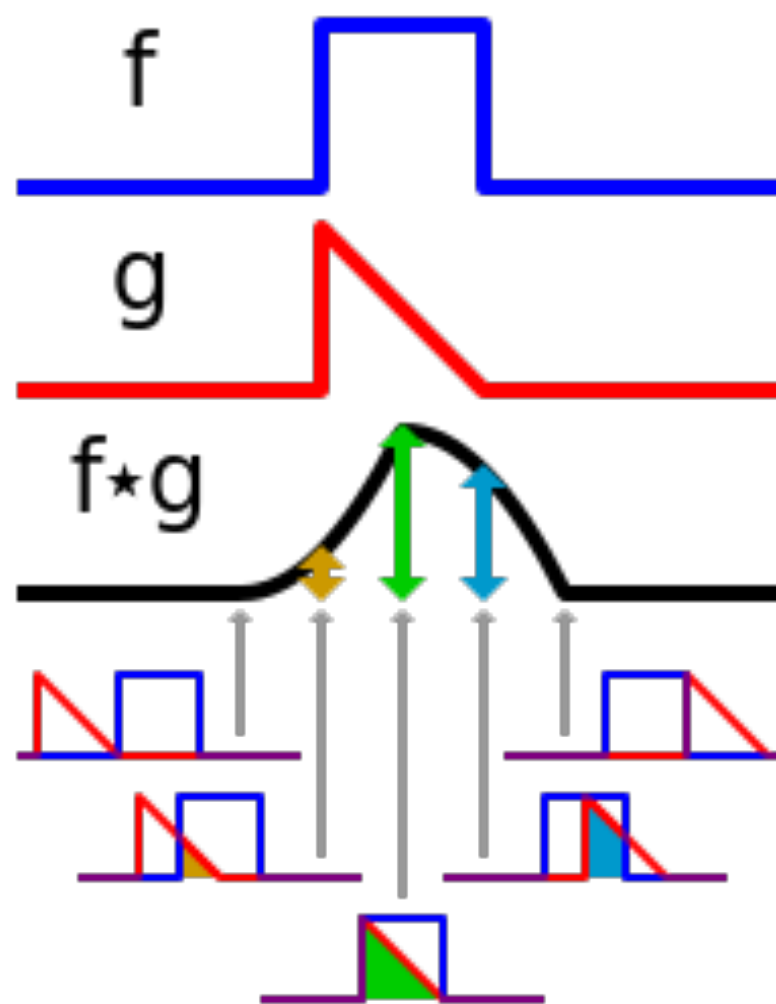
STARS OF DIGITAL SIGNAL PROCESSING

Filtering

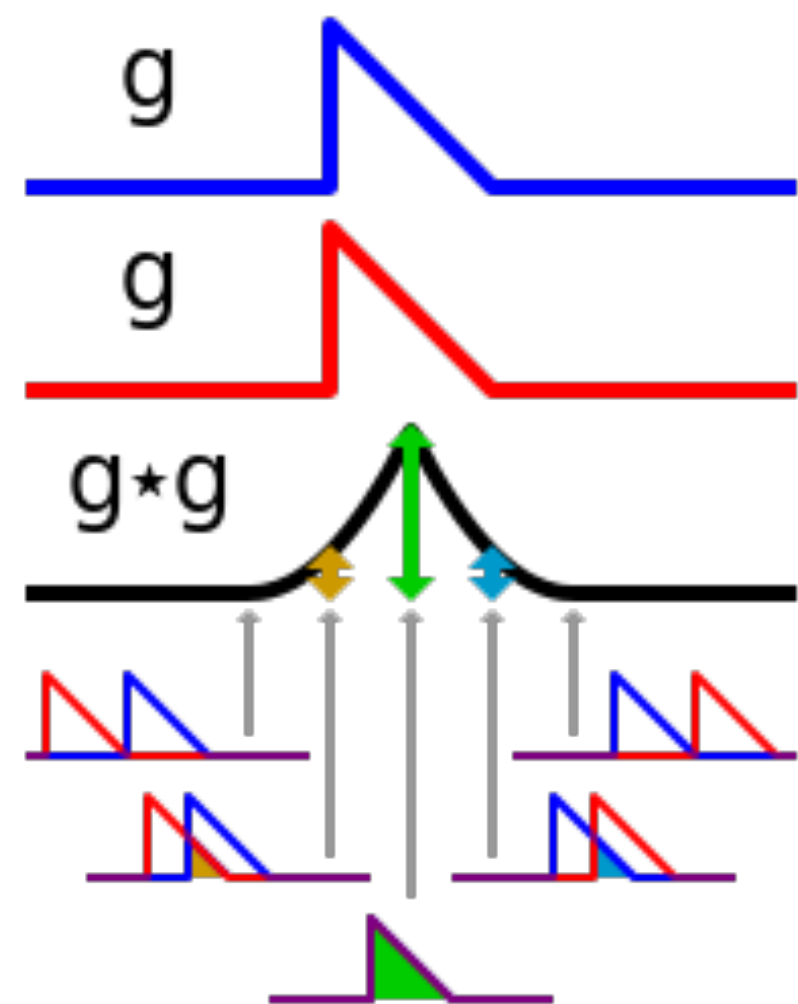
Convolution



Cross-correlation



Autocorrelation



STARS OF DIGITAL SIGNAL PROCESSING

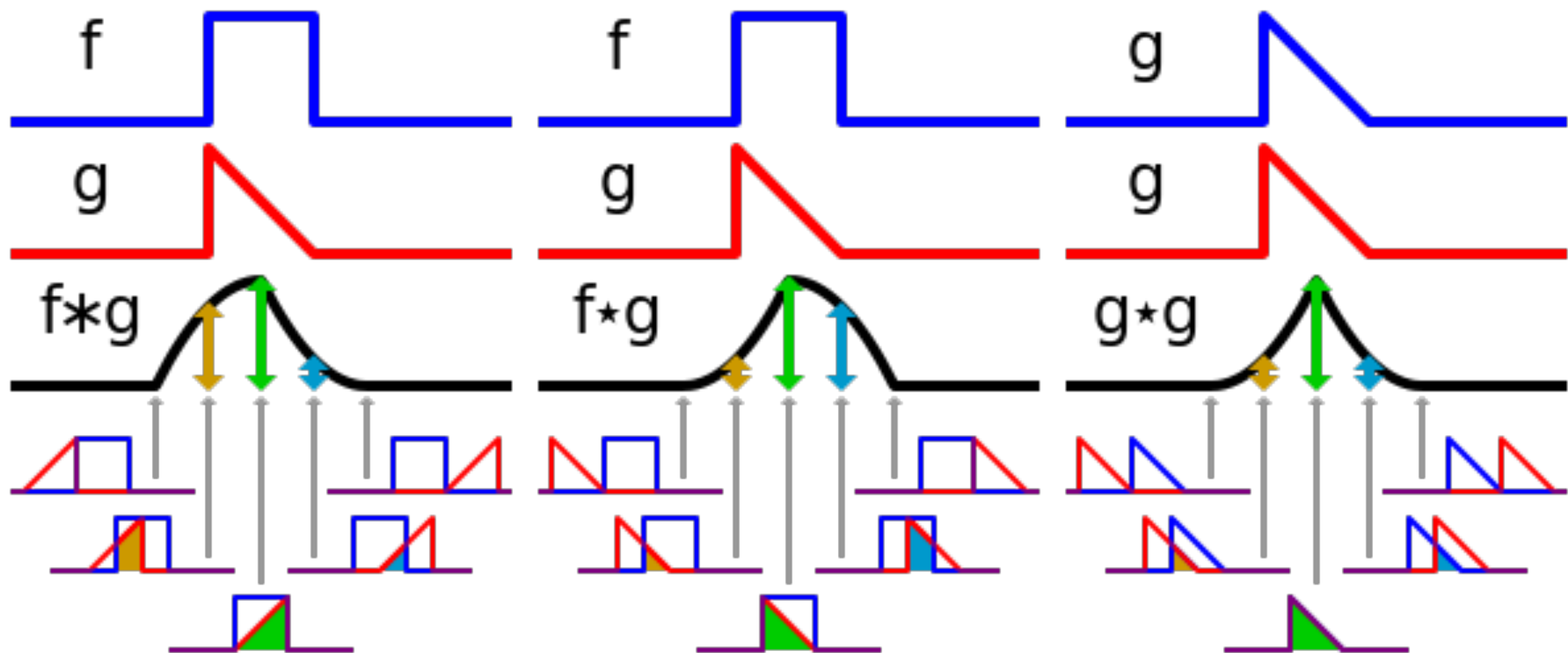
Filtering

Similarity detection

Convolution

Cross-correlation

Autocorrelation



STARS OF DIGITAL SIGNAL PROCESSING

Convolution

$$f(x) * g(x) = \int_{-\infty}^{\infty} f(\tau) \cdot g(x - \tau) d\tau$$

Cross-correlation

$$(f \star g)(t) \stackrel{\text{def}}{=} \int_{-\infty}^{\infty} f^*(\tau) g(t + \tau) d\tau,$$

WHAT'S WITH THE MINUS SIGN?

<https://www.oreilly.com/library/view/elegant-scipy/9781491922927/ch04.html#windowing>

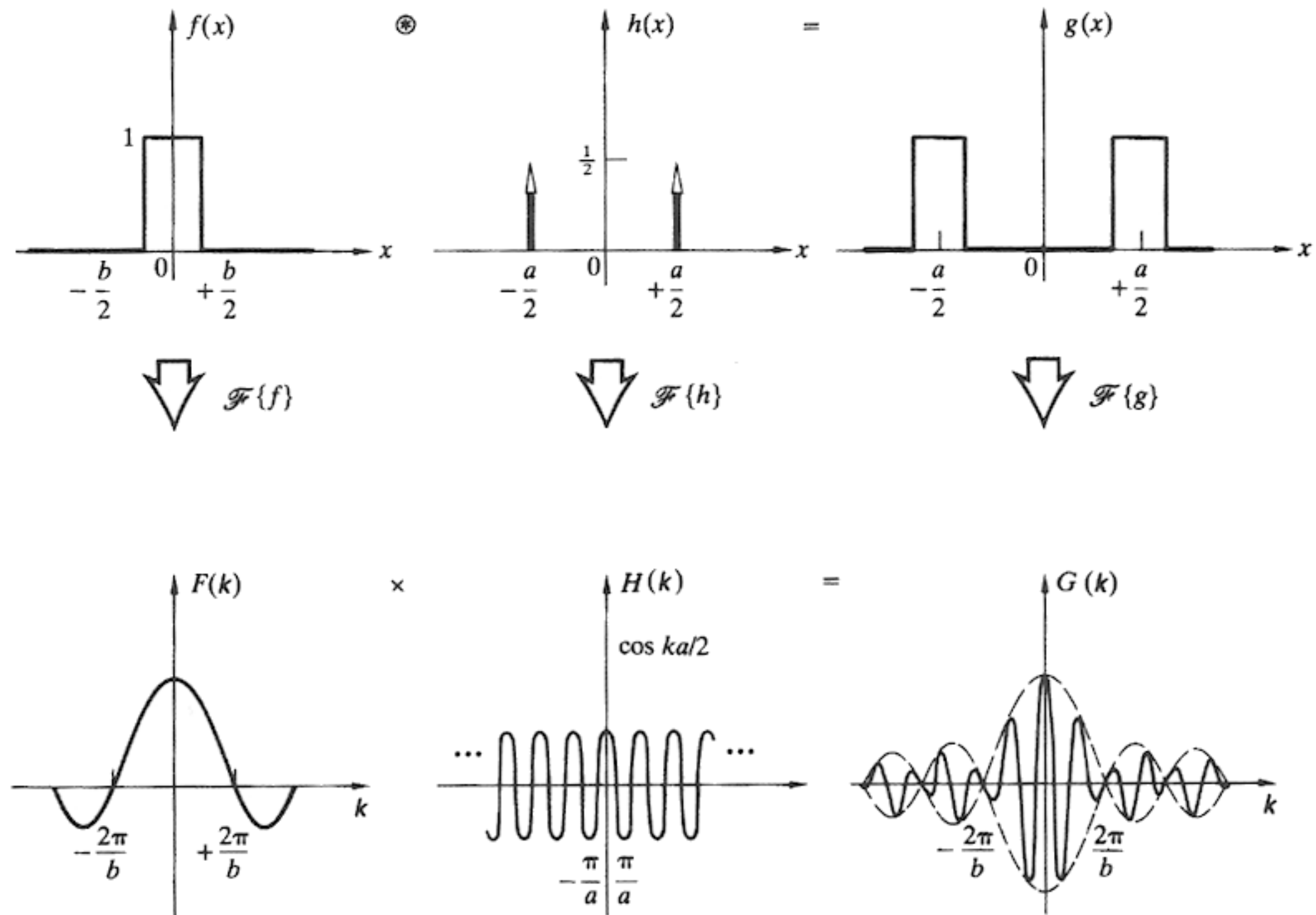
The effect of windowing our previous example is noticeable:

```
win = np.kaiser(len(t), 5)
X_win = fftpack.fft(x * win)

plt.plot(fftpack.fftfreq(len(t)), np.abs(X_win))
plt.ylim(0, 190);
```

**Convolution in time domain
=
Multiplication in frequency domain!
(and vice versa)**

HOW IS CONVOLUTION LIKE MULTIPLICATION?



FILTERING (OSGOOD NOTES. 3.4.1)

Lowpass filters An ideal *lowpass filter* cuts off all frequencies *above* a certain amount ν_c (“c” for “cutoff”) and lets all frequencies *below* ν_c pass through unchanged. (Hence the description “lowpass”.) If we write the operation as

$$w(t) = (h * v)(t) \iff W(s) = H(s)V(s),$$

then the transfer function we want is

$$H(s) = \begin{cases} 1 & |s| < \nu_c \\ 0 & |s| \geq \nu_c \end{cases}$$

Multiplying $V(s)$ by $H(s)$ leaves unchanged the spectrum of v for $|s| < \nu_c$ and eliminates the other frequencies. The transfer function is just a scaled rect function, and we can write it (to remind you) as

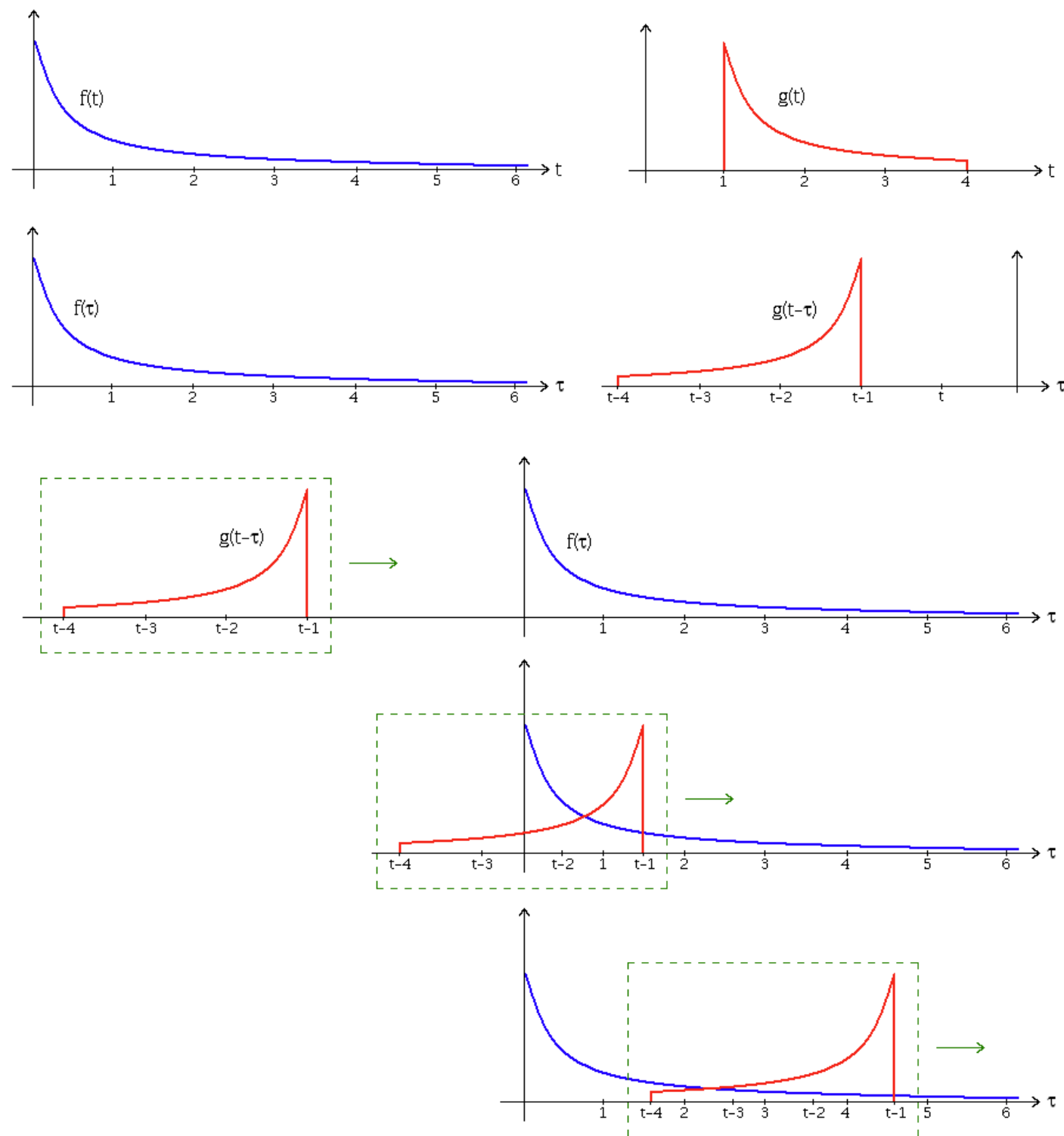
$$H(s) = \Pi_{2\nu_c}(s) = \Pi(s/2\nu_c) = \begin{cases} 1 & |s/2\nu_c| < \frac{1}{2} \\ 0 & |s/2\nu_c| \geq \frac{1}{2} \end{cases} = \begin{cases} 1 & |s| < \nu_c \\ 0 & |s| \geq \nu_c \end{cases}$$

In the time domain the impulse response is the inverse Fourier transform of $\Pi_{2\nu_c}$, and this is

$$h(t) = 2\nu_c \operatorname{sinc}(2\nu_c t).$$

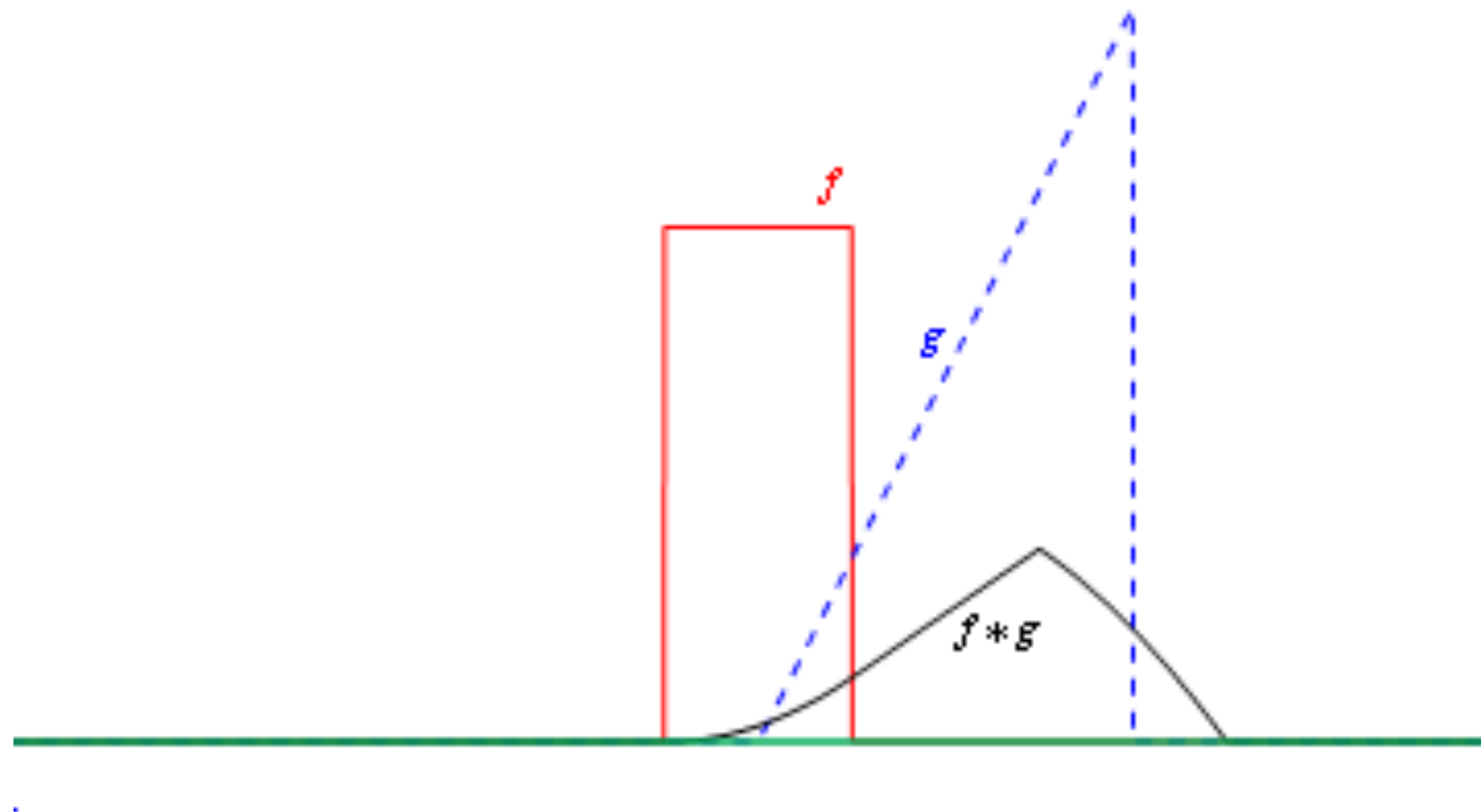
FLIP AND SHIFT!

<https://commons.wikimedia.org/wiki/Category:Convolution#/media/File:Convolution3.PNG>



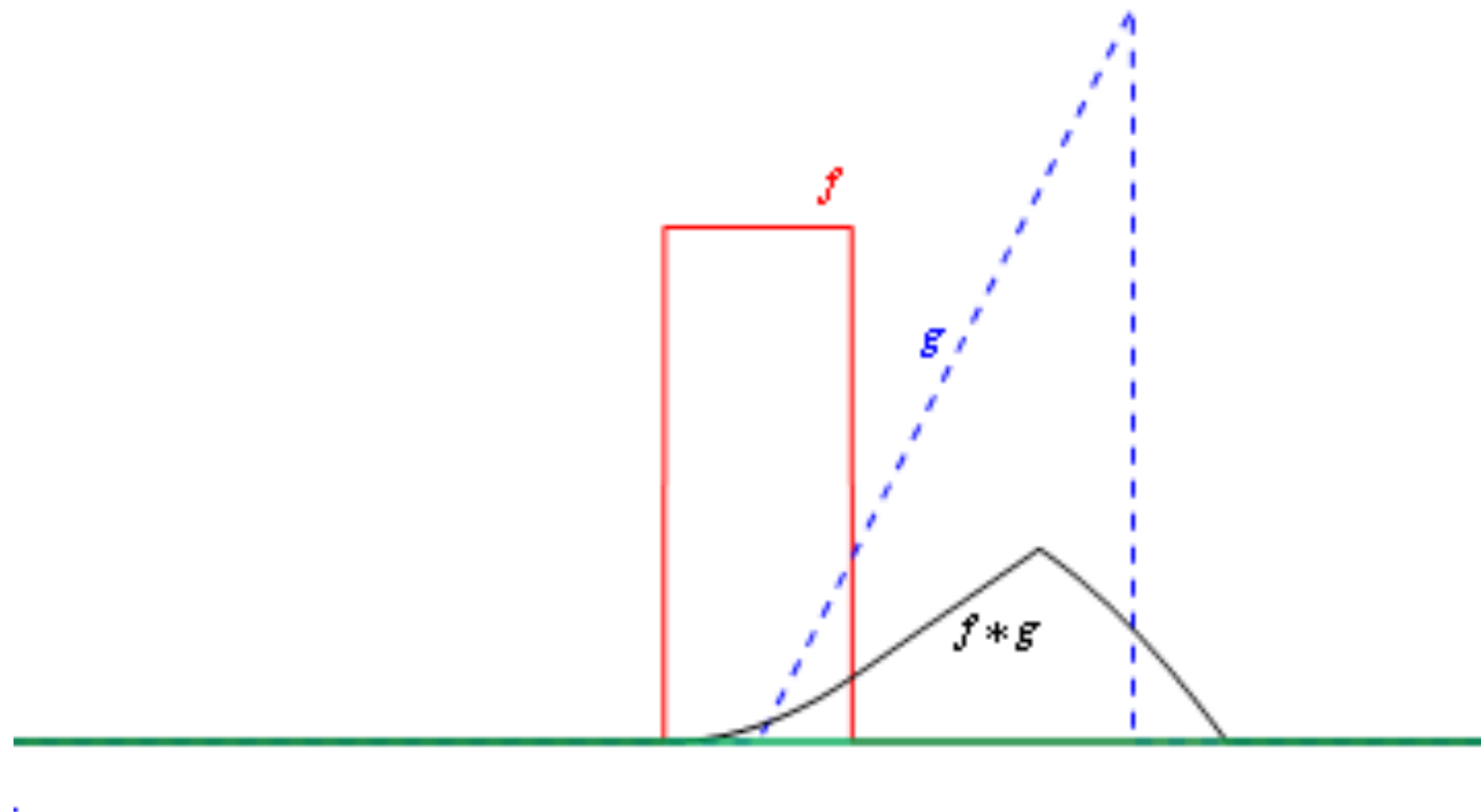
FLIP AND SHIFT! RECT AND RAMP

https://upload.wikimedia.org/wikipedia/commons/f/f8/Convolution_Animation_%28Boxcar_and_Ramp%29.gif



FLIP AND SHIFT! RECT AND RAMP

https://upload.wikimedia.org/wikipedia/commons/f/f8/Convolution_Animation_%28Boxcar_and_Ramp%29.gif



What happens when you convolve a rect function with itself three times? Four times? Five times? etc.?

What happens when you convolve a Gaussian function with some other Gaussian function? three times? Four times? Five times? etc.?

DIGITAL CONVOLUTION

One Way to Think of Convolution

$$x(t) * h(t) = \int_{-\infty}^{\infty} x(\tau) h(t - \tau) d\tau$$

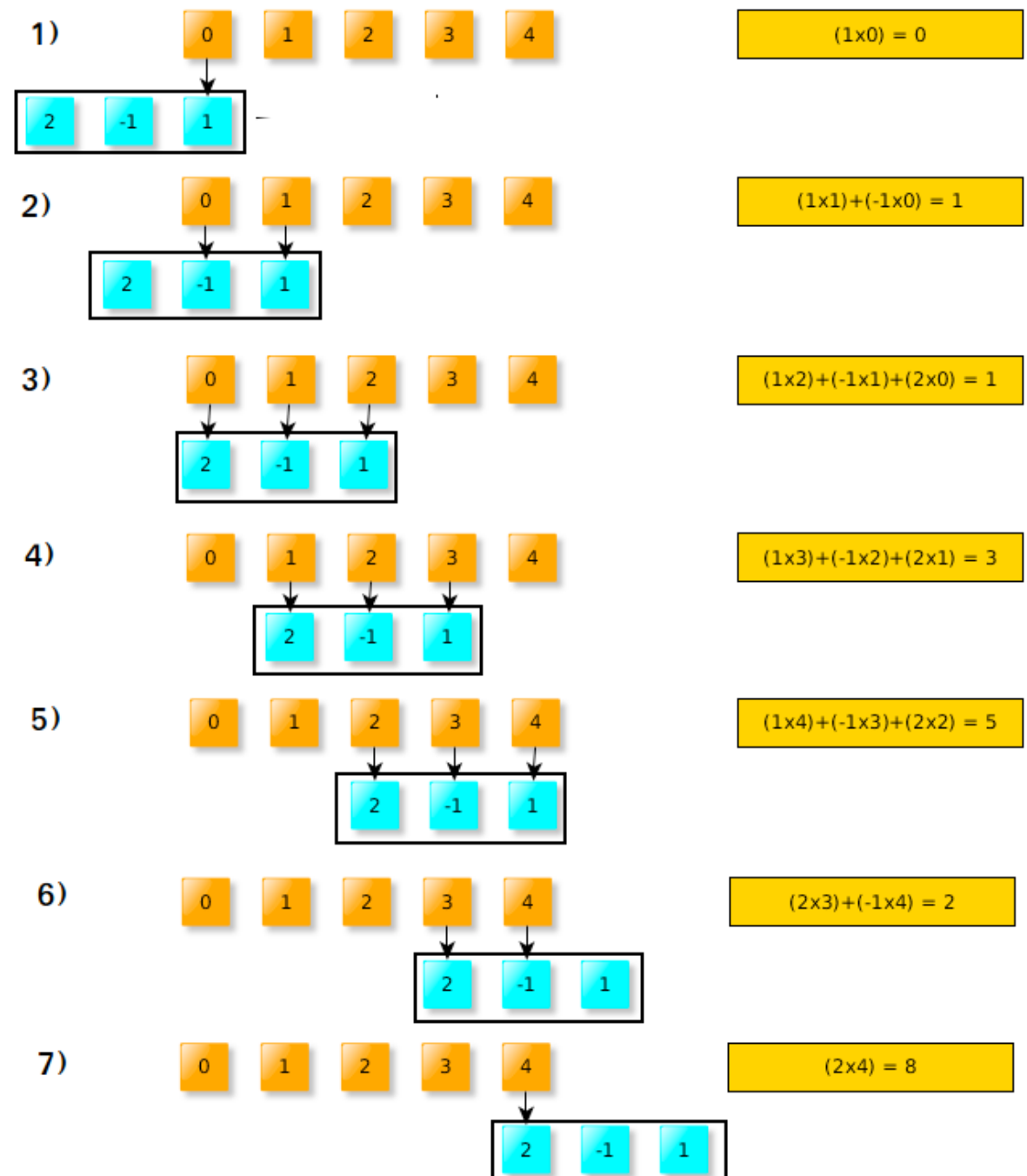
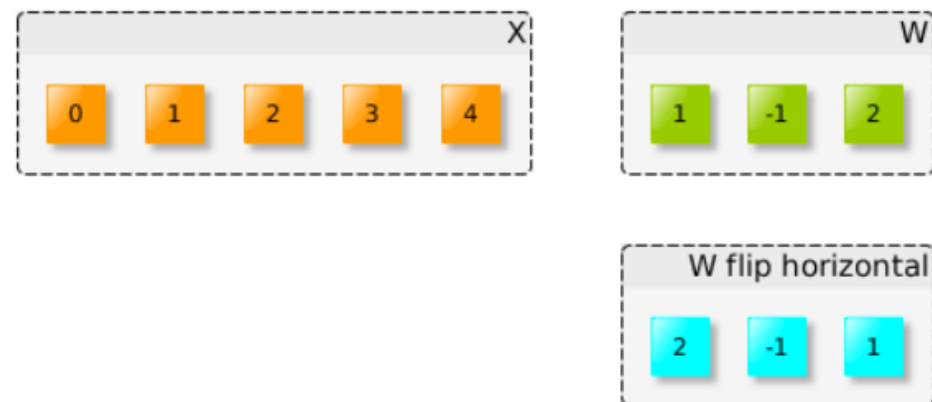
$$x[j] * h[j] = \sum_k x[k] \cdot h[j - k]$$

Think of it this way:

- Shift a copy of h to each position t (or discrete position k)
- Multiply by the value at that position $x(t)$ (or discrete sample $x[k]$)
- Add shifted, multiplied copies for all t (or discrete k)

FOR A WORKED OUT NUMERICAL EXAMPLE...

<https://leonardoaraujosantos.gitbooks.io/artificial-intelligence/content/convolution.html>



FOR A WORKED OUT NUMERICAL EXAMPLE...

<https://leonardoaraujosantos.gitbooks.io/artificial-intelligence/content/convolution.html>

```
In [1]: import numpy as np
In [2]: x = np.array([0,1,2,3,4])
In [3]: w = np.array([1,-1,2])
In [4]: res = np.convolve(x,w)
In [5]: print res
[0 1 1 3 5 2 8]
```